# $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$, a New Barium Vanadium(V) Phosphate Hydrate Containing Trigonal Bipyramidal $\mathrm{VO}_{5}$ Groups 

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#### Abstract

The hydrothermal synthesis, single crystal structure, and some physical properties of $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$, a new barium vanadium $(\mathrm{V})$ phosphate hydrate, are reported. This phase is built up from one-dimensional chains of unusual $\mathrm{VO}_{5}$ trigonal bipyramids and ( H$) \mathrm{PO}_{4}$ tetrahedra, fused together via $\mathrm{V}-\mathrm{O}-\mathrm{P}$ linkages. These anionic chains propagate along the polar [010] direction. 11-Coordinate barium cations and water molecules occupy the interchain regions and link the chains together. Structural data for this phase and other known barium vanadium phosphates are briefly compared. Crystal data: $\mathbf{B a}_{2}\left(\mathrm{VO}_{2}\right)$ $\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}, M_{\mathrm{r}}=566.57$, monoclinic, space group $\mathrm{P2}_{1}$ (No. 4), $a=5.0772(5) \AA, b=8.724(2) \AA, c=10.806(1) \AA, \beta=$ 90.795(8) ${ }^{\circ}, V=478.6(1) \AA^{3}, Z=2, R=2.65 \%, R_{\mathrm{w}}=2.89 \%[147$ parameters, 1893 observed reflections with $I>3 \sigma(I)]$. © 1998 Academic Press


## INTRODUCTION

A number of barium vanadium phosphates (BaVPOs) have now been prepared and structurally characterized on the basis of single crystal diffraction data (1-14). As is typical of vanadium compounds, the V cations in these BaVPO phases show flexibility in both oxidation state [ $\mathrm{V}^{\text {III }}$, $\mathrm{V}^{\mathrm{IV}}$, or $\mathrm{V}^{\mathrm{V}}$ ] and coordination preference, leading to wide structural diversity in these materials (vide infra). The first mixed-valence [ $\mathrm{V}^{\mathrm{IV}}$ and $\mathrm{V}^{\mathrm{V}}$ ] BaVPOs have been described very recently $(13,14)$.

In this paper we report the hydrothermal synthesis and single crystal structural characterization of $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)$ $\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$, a new colorless, noncentrosymmetric barium vanadium $(\mathrm{V})$ phosphate hydrate which contains unusual $\mathrm{VO}_{5}$ trigonal bipyramids as a component part of one-dimensional $\left[\mathrm{VO}_{2}\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right)\right]^{4-}$ anionic chains. The structures of known BaVPO phases are briefly compared.

[^0]
## EXPERIMENTAL

Synthesis and initial characterization. $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)$ $\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ was prepared from a mixture of $\mathrm{BaCO}_{3}$ $(2.19 \mathrm{~g}), 85 \% \mathrm{H}_{3} \mathrm{PO}_{4}(6.40 \mathrm{~g}), \mathrm{V}_{2} \mathrm{O}_{5}(0.25 \mathrm{~g})$, and 10 mL deionized water (starting molar ratio of $\mathrm{Ba}: \mathrm{V}: \mathrm{P}=4: 1: 20$ ). These components were sealed in a $23-\mathrm{ml}$ capacity Teflonlined hydrothermal bomb and heated to $120^{\circ} \mathrm{C}$ for 17 h . After slow cooling, the bomb was opened, and the solid contents recovered by vacuum filtration, resulting in a mixture of at least three types of visually distinct crystals - very pale yellowish blocks of $\mathrm{BaHPO}_{4}$ (15), small transparent crystals of $\mathrm{NH}_{4} \mathrm{VO}_{3}$ (16), and intergrown transparent plate-like crystals of the title compound. Visual estimation of the yield of $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ in this mixture was in the $5-10 \%$ range. We have not succeeded in preparing $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ in higher yield. Hydrothermal reactions starting from stoichiometric amounts of $\mathrm{Ba}-$, V-, and P-containing precursors led to insignificant amounts of the title compound.

X-ray powder diffraction data [Siemens D5000 automated diffractometer, $\mathrm{CuK} \alpha$ radiation, $\lambda=1.5418 \AA, T=$ $25(2)^{\circ} \mathrm{C}$ ] were recorded for a well-ground powder sample of $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ (hand-separated crystals from the as-synthesized mixture). The use of software "stripping" and peak-fitting routine established peak positions relative to the $\mathrm{Cu} K \alpha_{1}(\lambda=1.54056 \AA)$ wavelength. The data were indexed by comparison with a LAZY-PULVERIX (17) simulation of the single crystal structure of $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)$ $\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$, and least-squares refinement was carried out with the program ERACEL (18) to result in monoclinic cell parameters of $a=5.066(3) \AA, b=8.725(2) \AA, c=10.801(4) \AA$, and $\beta=90.80(3)^{\circ}\left(V=477.4 \AA^{3}\right)$. Powder data for $\mathrm{Ba}_{2}$ $\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ are listed in Table 1.

Thermogravimetric data for the title compound were collected on a Rigaku Thermoflex system. The sample was heated at a ramp rate of $20^{\circ} \mathrm{C} / \mathrm{min}$ under flowing oxygen. Infrared data were collected from 4000 to $400 \mathrm{~cm}^{-1}$ using a Matteson FTIR spectrometer ( KBr disk method).

TABLE 1
Powder Data for $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$

| $h$ | $k$ | $l$ | $d_{\text {obs }}(\AA)$ | $d_{\text {calc }}(\AA)$ | $\Delta d$ | $I_{\text {rel }}$ |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| 0 | 0 | 1 | 10.767 | 10.800 | -0.033 | 3 |
| 0 | 1 | 1 | 6.789 | 6.787 | 0.002 | 33 |
| 0 | 0 | 2 | 5.399 | 5.400 | -0.001 | 27 |
| 1 | 0 | 0 | 5.066 | 5.066 | 0.001 | 13 |
| 0 | 2 | 0 | 4.366 | 4.362 | 0.004 | 13 |
| 0 | 2 | 1 | 4.046 | 4.045 | 0.001 | 26 |
| 1 | 0 | 2 | 3.669 | 3.669 | -0.001 | 21 |
| 0 | 0 | 3 | 3.602 | 3.600 | 0.002 | 33 |
| 1 | 1 | -2 | 3.422 | 3.422 | 0.000 | 96 |
| 1 | 1 | 2 | 3.381 | 3.382 | -0.002 | 100 |
| 1 | 2 | 0 | 3.306 | 3.306 | 0.000 | 28 |
| 1 | 2 | -1 | 3.166 | 3.169 | -0.003 | 72 |
| 1 | 0 | -3 | 2.957 | 2.954 | 0.003 | 13 |
| 1 | 0 | 3 | 2.917 | 2.915 | 0.001 | 9 |
| 1 | 2 | -2 | 2.832 | 2.831 | 0.002 | 15 |
| 0 | 3 | 1 | 2.807 | 2.808 | -0.001 | 54 |
| 0 | 1 | 4 | 2.580 | 2.579 | 0.001 | 51 |
| 0 | 3 | 3 | 2.262 | 2.262 | 0.000 | 29 |
| 0 | 4 | 1 | 2.138 | 2.138 | 0.000 | 23 |
| 1 | 2 | -4 | 2.099 | 2.100 | -0.002 | 36 |
| 1 | 3 | 3 | 2.058 | 2.059 | -0.001 | 19 |
| 1 | 4 | 1 | 1.969 | 1.968 | 0.001 | 13 |
| 1 | 1 | 5 | 1.928 | 1.928 | 0.000 | 12 |
| 1 | 4 | -2 | 1.881 | 1.882 | 0.000 | 16 |
| 2 | 3 | -3 | 1.695 | 1.695 | 0.000 | 11 |
| 1 | 5 | 2 | 1.576 | 1.576 | 0.000 | 12 |

Single-crystal structure determination. A transparent plate (dimensions $\sim 0.1 \times 0.3 \times 0.4 \mathrm{~mm}$ ) of $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)$ $\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ was glued to a thin glass fiber with cyanoacrylate adhesive and mounted on a Siemens P4 automated diffractometer (graphite-monochromated $\operatorname{Mo} K \alpha$ radiation, $\lambda=0.71073 \AA ̊)$. A primitive monoclinic unit cell was established and optimized by the application of peak-search, centering, indexing, and least-squares routines ( 54 peaks, $10<2 \theta<25^{\circ}$ ).
Intensity data were collected at room temperature [25(2) $\left.{ }^{\circ} \mathrm{C}\right]$ using the $\theta / 2 \theta$ scan mode for $2<2 \theta<65^{\circ}$ $(-1 \leq h \leq 7,-1 \leq k \leq 13,-16 \leq l \leq 16)$. Intensity standards, remeasured every 100 observations, showed only statistical fluctuations over the course of the data collection. Absorption was monitored by $\psi$ scans, and a correction ( $\min 0.451$, max 0.755 ) was applied at the data reduction stage. The raw intensities were reduced to $F$ and $\sigma(F)$ values, the normal corrections for Lorentz and polarization effects were made, and the equivalent data were averaged: 2237 measured reflections merged to 2029 unique data [1893 considered observed according to the criterion $I>3 \sigma(I)]$ with $R_{\text {Int }}=2.84 \%$.

The systematic absence condition in the reduced data ( $0 k 0, k \neq 2 n$ ) indicated space group $P 2_{1}$ or $P 2_{1} / m$, with
intensity statistics suggesting the former. The main details of the $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ structure were established by Patterson methods (19) in space group $P 2_{1}$ (No. 4). No reasonable starting atomic model could be established in space group $P 2_{1} / m$, thus the noncentrosymmetric space group was assumed for the remainder of the refinement. The other non-hydrogen atoms were readily located from difference Fourier maps. Assuming the sole presence of vanadium $(\mathrm{V})$ in this phase, the charge balancing requirement necessitates the presence of three protons per formula unit. We assume that one water molecule and one $\mathrm{P}-\mathrm{OH}$ vertex account for the locations of these hydrogen atoms. These H atoms could not be located in difference Fourier syntheses; the hydrogen phosphate proton was placed geometrically (see below). Final residuals of $R=2.65 \%$ and $R_{\mathrm{w}}=2.89 \%\left[w_{\mathrm{i}}=1 / \sigma^{2}(F)\right]$ were obtained for refinements, varying a Larson-type extinction parameter (20), the Flack absolute structure parameter (21), and positional and anisotropic thermal parameters for all the atoms. The significant features in the final Fourier difference map were close to the Ba cations. The Flack parameter refined to $-0.05(2)$; thus the absolute structure of this phase is as shown in the Results section. Assuming the opposite absolute structure (Flack parameter fixed at 1.00) resulted in higher residuals of $R=3.03 \%$ and $R_{\mathrm{w}}=3.45 \%$. All the least-squares refinements and subsidiary calculations were performed with the Oxford CRYSTALS (22) system. Crystallographic data are summarized in Table 2.

TABLE 2
Crystallographic Parameters for $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathbf{H P O}_{4}\right) \cdot \mathbf{H}_{\mathbf{2}} \mathrm{O}$

| Empirical formula | $\mathrm{Ba}_{2} \mathrm{VP}_{2} \mathrm{O}_{11} \mathrm{H}_{3}$ |
| :--- | :--- |
| Formula weight | 566.57 |
| Crystal system | Monoclinic |
| $a(\AA)$ | $5.0772(5)$ |
| $b(\AA)$ | $8.724(2)$ |
| $c(\AA)$ | $10.806(1)$ |
| $\beta(\mathrm{deg})$ | $90.795(8)$ |
| $V\left(\AA^{3}\right)$ | $478.6(1)$ |
| $Z$ | 2 |
| Space group | $P 2_{1}(\mathrm{No} 4)$. |
| $T\left({ }^{\circ} \mathrm{C}\right)$ | $25(2)$ |
| $\lambda(\mathrm{MoK} \alpha)(\AA)$ | 0.71073 |
| $\rho_{\text {calc }}\left(\mathrm{g} / \mathrm{cm}^{3}\right)$ | 3.93 |
| $\mu\left(\mathrm{~cm}{ }^{-1}\right)$ | 94.5 |
| Total no. of data | 2237 |
| No. of observed data ${ }^{a}$ | 1893 |
| No. of Parameters | 147 |
| Min, max $\Delta \rho\left(\mathrm{e} / \AA^{3}\right)$ | $-1.4,+2.0$ |
| $R(F)^{b}(\%)$ | 2.65 |
| $R_{\mathrm{w}}(F)^{c}(\%)$ | 2.89 |

[^1]
## RESULTS

Crystal structure of $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$. Atomic positional and thermal parameters are listed in Table 3, and selected geometrical data are presented in Table 4. This material adopts a new crystal structure built up from 11coordinate barium cations, water molecules, and chains of vertex-sharing $\mathrm{VO}_{5}$ trigonal bipyramids and tetrahedral $\mathrm{PO}_{4} / \mathrm{HPO}_{4}$ units, fused together via $\mathrm{V}-\mathrm{O}-\mathrm{P}$ bonds. The crystal structure of $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ is illustrated (23) in Fig. 1.

There are 16 unique non-hydrogen atoms in $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)$ $\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$. The two barium cations both adopt irregular 11 -fold coordination (Figs. 2 and 3), assuming a cutoff of $3.5 \AA$ for the maximum $\mathrm{Ba}-\mathrm{O}$ distance. Average $\mathrm{Ba}-\mathrm{O}$ distances of $2.978(6)$ and $2.975(6) \AA$ result for $\mathrm{Ba}(1)$ and $\mathrm{Ba}(2)$, respectively. $\mathrm{Ba}(1)$ includes two water molecules [atom $\mathrm{O}(11)$ ] in its coordination sphere. Bond valence sums (BVS) calculated by the Brown formalism (24) of 2.04 for $\mathrm{Ba}(1)$ and 1.85 for $\mathrm{Ba}(2)$ (expected value $=2.00$ ) show that $\mathrm{Ba}(1)$ satisfies its valence requirement, whereas $\mathrm{Ba}(2)$ is slightly "underbonded" in this structure.
The single vanadium species in $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)$ $\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ adopts a distinctive distorted trigonal bipyramidal coordination with respect to its five O atom neighbors (Fig. 4). Two short ( $d<1.65 \AA$ ) bonds to $\mathrm{O}(1)$ and $\mathrm{O}(2)$ form two of the three equatorial vertices of this polyhedron $\left[\theta\{\mathrm{O}(1)-\mathrm{V}-\mathrm{O}(2)\}=106.3(3)^{\circ}\right]$. The three remaining vertices form parts of $\mathrm{V}-\mathrm{O}-\mathrm{P}$ links, with a resulting $\mathrm{O}-\mathrm{V}-\mathrm{O}$ bond angle of $160.8(2)^{\circ}$ for the two axial links. The bond valence sum for V is 4.96 (expected value for vanadium( V )

TABLE 3
Atomic Coordinates/Thermal Factors for $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$

| Atom | $x$ | $y$ | $z$ | $U_{\mathrm{eq}}{ }^{a}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{Ba}(1)$ | $0.03246(8)$ | $0.49849(9)$ | $0.04342(4)$ | 0.0142 |
| $\mathrm{Ba}(2)$ | $0.00970(7)$ | $0.84018(9)$ | $0.38855(4)$ | 0.0124 |
| $\mathrm{~V}(1)$ | $0.4416(2)$ | $0.4996(2)$ | $0.3294(1)$ | 0.0098 |
| $\mathrm{P}(1)$ | $0.4870(3)$ | $0.7772(2)$ | $0.1456(2)$ | 0.0104 |
| $\mathrm{P}(2)$ | $0.4635(3)$ | $0.1491(2)$ | $0.4205(2)$ | 0.0094 |
| $\mathrm{O}(1)$ | $0.558(1)$ | $0.4136(7)$ | $0.2080(5)$ | 0.0202 |
| $\mathrm{O}(2)$ | $0.1320(9)$ | $0.5350(7)$ | $0.2985(5)$ | 0.0159 |
| $\mathrm{O}(3)$ | $0.548(1)$ | $0.7128(6)$ | $0.2777(5)$ | 0.0148 |
| $\mathrm{O}(4)$ | $0.376(1)$ | $0.3176(6)$ | $0.4346(5)$ | 0.0159 |
| $\mathrm{O}(5)$ | $0.673(1)$ | $0.5612(7)$ | $0.4716(5)$ | 0.0135 |
| $\mathrm{O}(6)$ | $0.628(1)$ | $0.9386(7)$ | $0.1472(5)$ | 0.0190 |
| $\mathrm{O}(7)$ | $0.607(1)$ | $0.6840(9)$ | $0.0454(5)$ | 0.0264 |
| $\mathrm{O}(8)$ | $0.1908(9)$ | $0.8025(7)$ | $0.1310(5)$ | 0.0173 |
| $\mathrm{O}(9)$ | $0.353(1)$ | $0.0817(7)$ | $0.2997(5)$ | 0.0183 |
| $\mathrm{O}(10)$ | $0.760(1)$ | $0.1339(7)$ | $0.4332(6)$ | 0.0221 |
| $\mathrm{O}(11)$ | $0.981(1)$ | $0.2117(7)$ | $0.1559(5)$ | 0.0193 |

[^2]TABLE 4
Selected Bond Distances ( $\AA$ ) and Angles ( ${ }^{\circ}$ ) for $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$

| $\mathrm{Ba}(1)-\mathrm{O}(1)$ | $3.105(5)$ | $\mathrm{Ba}(1)-\mathrm{O}(1)$ | $3.271(6)$ |
| :--- | ---: | :--- | ---: |
| $\mathrm{Ba}(1)-\mathrm{O}(2)$ | $2.813(5)$ | $\mathrm{Ba}(1)-\mathrm{O}(6)$ | $2.755(5)$ |
| $\mathrm{Ba}(1)-\mathrm{O}(7)$ | $2.699(6)$ | $\mathrm{Ba}(1)-\mathrm{O}(7)$ | $3.336(7)$ |
| $\mathrm{Ba}(1)-\mathrm{O}(7)$ | $3.442(8)$ | $\mathrm{Ba}(1)-\mathrm{O}(8)$ | $2.925(6)$ |
| $\mathrm{Ba}(1)-\mathrm{O}(8)$ | $2.775(5)$ | $\mathrm{Ba}(1)-\mathrm{O}(11)$ | $2.795(6)$ |
| $\mathrm{Ba}(1)-\mathrm{O}(11)$ | $2.846(6)$ | $\mathrm{Ba}(2)-\mathrm{O}(2)$ | $2.905(6)$ |
| $\mathrm{Ba}(2)-\mathrm{O}(3)$ | $2.845(5)$ | $\mathrm{Ba}(2)-\mathrm{O}(3)$ | $3.198(6)$ |
| $\mathrm{Ba}(2)-\mathrm{O}(4)$ | $2.763(5)$ | $\mathrm{Ba}(2)-\mathrm{O}(5)$ | $3.113(6)$ |
| $\mathrm{Ba}(2)-\mathrm{O}(5)$ | $2.920(5)$ | $\mathrm{Ba}(2)-\mathrm{O}(6)$ | $3.340(6)$ |
| $\mathrm{Ba}(2)-\mathrm{O}(8)$ | $2.961(5)$ | $\mathrm{Ba}(2)-\mathrm{O}(9)$ | $2.906(6)$ |
| $\mathrm{Ba}(2)-\mathrm{O}(10)$ | $2.902(6)$ | $\mathrm{Ba}(2)-\mathrm{O}(10)$ | $2.873(6)$ |
| $\mathrm{V}(1)-\mathrm{O}(1)$ | $1.629(6)$ | $\mathrm{V}(1)-\mathrm{O}(2)$ | $1.632(5)$ |
| $\mathrm{V}(1)-\mathrm{O}(3)$ | $2.017(6)$ | $\mathrm{V}(1)-\mathrm{O}(4)$ | $1.983(6)$ |
| $\mathrm{V}(1)-\mathrm{O}(5)$ | $1.996(5)$ | $\mathrm{P}(1)-\mathrm{O}(3)$ | $1.560(5)$ |
| $\mathrm{P}(1)-\mathrm{O}(6)$ | $1.579(6)$ | $\mathrm{P}(1)-\mathrm{O}(7)$ | $1.492(6)$ |
| $\mathrm{P}(1)-\mathrm{O}(8)$ | $1.526(5)$ | $\mathrm{P}(2)-\mathrm{O}(4)$ | $1.544(6)$ |
| $\mathrm{P}(2)-\mathrm{O}(5)$ | $1.566(6)$ | $\mathrm{P}(2)-\mathrm{O}(9)$ | $1.530(6)$ |
| $\mathrm{P}(2)-\mathrm{O}(10)$ | $1.516(5)$ |  |  |
|  |  |  |  |
| $\mathrm{O}(1)-\mathrm{V}(1)-\mathrm{O}(2)$ | $106.3(3)$ | $\mathrm{O}(1)-\mathrm{V}(1)-\mathrm{O}(3)$ | $95.8(3)$ |
| $\mathrm{O}(2)-\mathrm{V}(1)-\mathrm{O}(3)$ | $91.7(3)$ | $\mathrm{O}(1)-\mathrm{V}(1)-\mathrm{O}(4)$ | $99.1(3)$ |
| $\mathrm{O}(2)-\mathrm{V}(1)-\mathrm{O}(4)$ | $95.7(3)$ | $\mathrm{O}(3)-\mathrm{V}(1)-\mathrm{O}(4)$ | $160.8(2)$ |
| $\mathrm{O}(1)-\mathrm{V}(1)-\mathrm{O}(5)$ | $121.9(3)$ | $\mathrm{O}(2)-\mathrm{V}(1)-\mathrm{O}(5)$ | $131.5(3)$ |
| $\mathrm{O}(3)-\mathrm{V}(1)-\mathrm{O}(5)$ | $78.9(2)$ | $\mathrm{O}(4)-\mathrm{V}(1)-\mathrm{O}(5)$ | $82.9(2)$ |
| $\mathrm{O}(3)-\mathrm{P}(1)-\mathrm{O}(6)$ | $103.2(3)$ | $\mathrm{O}(3)-\mathrm{P}(1)-\mathrm{O}(7)$ | $113.0(4)$ |
| $\mathrm{O}(6)-\mathrm{P}(1)-\mathrm{O}(7)$ | $107.7(4)$ | $\mathrm{O}(3)-\mathrm{P}(1)-\mathrm{O}(8)$ | $109.2(3)$ |
| $\mathrm{O}(6)-\mathrm{P}(1)-\mathrm{O}(8)$ | $108.5(3)$ | $\mathrm{O}(7)-\mathrm{P}(1)-\mathrm{O}(8)$ | $114.6(3)$ |
| $\mathrm{O}(4)-\mathrm{P}(2)-\mathrm{O}(5)$ | $105.2(3)$ | $\mathrm{O}(4)-\mathrm{P}(2)-\mathrm{O}(9)$ | $110.3(3)$ |
| $\mathrm{O}(5)-\mathrm{P}(2)-\mathrm{O}(9)$ | $106.6(3)$ | $\mathrm{O}(4)-\mathrm{P}(2)-\mathrm{O}(10)$ | $111.1(3)$ |
| $\mathrm{O}(5)-\mathrm{P}(2)-\mathrm{O}(10)$ | $109.9(3)$ | $\mathrm{O}(9)-\mathrm{P}(2)-\mathrm{O}(10)$ | $113.3(3)$ |
| $\mathrm{V}(1)-\mathrm{O}(3)-\mathrm{P}(1)$ | $122.3(3)$ | $\mathrm{V}(1)-\mathrm{O}(4)-\mathrm{P}(2)$ | $130.9(3)$ |
| $\mathrm{V}(1)-\mathrm{O}(5)-\mathrm{P}(2)$ | $116.3(3)$ |  |  |
|  |  |  |  |

character $=5.00$ ). The $\mathrm{VO}_{5}$ polyhedron is somewhat distorted. Axial-equatorial $\mathrm{O} \cdots \mathrm{O}$ contacts cover a fairly narrow range from 2.55 to $2.76 \AA$ (average $=2.66 \AA$ ); however, the equatorial $\mathrm{O} \cdots \mathrm{O}$ contact between $\mathrm{O}(1)$ and $\mathrm{O}(2)$ $(2.61 \AA)$ is much shorter than the $\mathrm{O}(1) \cdots \mathrm{O}(3)$ and $\mathrm{O}(2) \cdots \mathrm{O}(3)$ nonbonding contacts ( 3.17 and $3.31 \AA$, respectively). Within the $\mathrm{O}_{5}$ polyhedron (volume $=5.09 \AA^{3}$ ), the V atom has made a nominal shift of $0.143 \AA$ from the centroid (25) of this group towards an equatorial edge, resulting in the two short $\mathrm{V}=\mathrm{O}$ links noted above. The equatorial $\mathrm{V}(1), \mathrm{O}(1), \mathrm{O}(2), \mathrm{O}(5)$ grouping is planar to within 0.06 Å.

The phosphorus atoms show typical tetrahedral coordination $\left[d_{\mathrm{av}}(\mathrm{P}(1)-\mathrm{O})=1.539(5) \AA\right.$, $\mathrm{BVS}[\mathrm{P}(1)]=4.96 ; d_{\mathrm{av}}(\mathrm{P}(2)-$ $\mathrm{O})=1.539(5) \AA, \quad \mathrm{BVS}[\mathrm{P}(2)]=4.95]$. The $\mathrm{P}(1)$ centered group makes one $\mathrm{P}-\mathrm{O}-\mathrm{V}$ link and has three terminal $\mathrm{P}-\mathrm{O}$ bonds, one of which is assumed to be protonated, as $\mathrm{P}(1)-\mathrm{O}(6) \mathrm{H}$, on the basis of its length (26). The $\mathrm{P}(2) \mathrm{O}_{4}$ group makes two $\mathrm{P}-\mathrm{O}-\mathrm{V}$ links, and has two terminal $\mathrm{P}-\mathrm{O}$ bonds. There is one water molecule of crystallization [oxygen atom $\mathrm{O}(11)]$.


FIG. 1. View down [100] of the crystal structure of $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ showing the infinite $\left[\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right)\right]^{4-}$ chain. The proposed intrachain H bonding linkage is indicated as a thin line. $\mathrm{Ba}-\mathrm{O}$ bonds are omitted for clarity ( $50 \%$ thermal ellipsoids; arbitrary sphere for H atom).

Of the 11 O atoms in the structure, $\mathrm{O}(1)$ and $\mathrm{O}(2)$ are terminal to V and may be regarded as parts of $\mathrm{V}=\mathrm{O}$ "vanadyl" double bonds. Their individual bond valences are more than double those of the longer V-O bonds. Atoms $\mathrm{O}(3), \mathrm{O}(4)$, and $\mathrm{O}(5)$ form $\mathrm{V}-\mathrm{O}-\mathrm{P}$ bridges $\left(\theta_{\mathrm{av}}=123.2^{\circ}\right)$, and $\mathrm{O}(6)-\mathrm{O}(10)$ are terminal $\mathrm{P}-\mathrm{O}$ vertices, all of which also form part of one or more $\mathrm{Ba}-\mathrm{O}$ contacts. The water molecule oxygen atom, $\mathrm{O}(11)$, bonds to two $\mathrm{Ba}(1)$ cations and has contacts to $\mathrm{O}(9) \quad[d(\mathrm{O} \cdots \mathrm{O})=2.681(8) \AA], \quad \mathrm{O}(1)$ $[2.840(8) \AA], \mathrm{O}(6)[2.985(9) \AA]$, and $\mathrm{O}(7)[3.048(7) \AA]$ which might represent H bonding links.

The polyhedral connectivity in $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot$ $\mathrm{H}_{2} \mathrm{O}$ results in contorted, infinite chains of $\mathrm{VO}_{5}$ and $\mathrm{P}(2) \mathrm{O}_{4}$


FIG. 2. Detail of the $\mathrm{Ba}(1)$ coordination environment in $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)$ $\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ with nonbonding $\mathrm{O} \cdots \mathrm{O}$ contacts $<4.0 \AA$ indicated by thin lines.
groups propagating along the polar [010] direction (Fig. 1). The $\mathrm{P}(1) \mathrm{O}_{4}$ group also bonds to the vanadium center, but it does not partake in the chain connectivity. Based on geometrical placement of the H atom, a strong intrachain hydrogen bond exists between two phosphate groups (Fig. 1), as an $\mathrm{O}(6)-\mathrm{H}(1) \cdots \mathrm{O}(9) \operatorname{link}[d(\mathrm{H} \cdots \mathrm{O})=1.50 \AA$ ]. However, when $\mathrm{P}-\mathrm{O}$ and $\mathrm{Ba}-\mathrm{O}$ interactions are taken into account, the bond valence sums of $\mathrm{O}(6)$ and $\mathrm{O}(9)$ are both $\sim 1.46$. Thus, the possibility of a symmetrical $\mathrm{O}(6) \cdots$ $\mathrm{H} \cdots \mathrm{O}(9)$ or disordered [both $\mathrm{O}(6)-\mathrm{H}(1) \cdots \mathrm{O}(9)$ and $\mathrm{O}(6) \cdots \mathrm{H}(1)-\mathrm{O}(9)$ conformations present] hydrogen bond cannot be ruled out. Interchain connectivity is through barium cations and possibly via H -bonding interactions


FIG. 3. Detail of the $\mathrm{Ba}(2)$ coordination environment in $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)$ $\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ with nonbonding $\mathrm{O} \cdots \mathrm{O}$ contacts $<4.0 \AA$ indicated by thin lines.


FIG. 4. Detail of the $\mathrm{VO}_{5}$ trigonal bipyramidal grouping in $\mathrm{Ba}_{2}$ $\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$.
involving the $\mathrm{O}(11)$ water molecule. Considered separately, the $\mathrm{Ba} / \mathrm{O}$ network includes triangular face-sharing and edge-sharing connectivity between the $\mathrm{BaO}_{11}$ polyhedra.

## Physical Data

TGA for $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ showed two endothermic weight loss events $(-3 \%$ over the temperature range $\sim 330-390^{\circ} \mathrm{C}$, and $-1.2 \%$ at $\sim 500-560^{\circ} \mathrm{C}$ ). The first of these probably corresponds to loss of the extrachain water molecule (calc. $-3.2 \%$ ), and the second may arise from breakdown of the $\mathrm{HPO}_{4}$ group to yield $\frac{1}{2} \mathrm{H}_{2} \mathrm{O}$ (calc. $-1.6 \%$ ), leaving a nominal residue of $\mathrm{Ba}_{2} \mathrm{VP}_{2} \mathrm{O}_{9.5}$. A third endotherm at $\sim 680^{\circ} \mathrm{C}$ was not accompanied by an observable weight change and may arise from a phase transformation or melting/decomposition.

The infrared spectrum of $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ (Fig. 5) shows bands due to $\mathrm{PO}_{4}$ and water modes in the region 2800-3200 and $3500 \mathrm{~cm}^{-1}$. The complex group of bands in the $800-1300 \mathrm{~cm}^{-1}$ region arises from partially resolved $\mathrm{PO}_{4}$ and VO modes.

## DISCUSSION

We have prepared and characterized another BaVPO phase, complementing the materials listed in Table 5. As is typical of the seemingly limitless structural diversity of vanadium phosphates, $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ shows no particular similarities to any of the previously characterized BaVPOs. A large excess of phosphoric acid was required to synthesize $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ in measurable yield, which perhaps signifies that the acid is


FIG. 5. IR spectrum of $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$.
playing a dual role in supplying phosphate ions and controlling pH in the hydrothermal reaction.

The trigonal bipyramidal geometry of the $\mathrm{VO}_{5}$ group in $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ is distinctive and unusual in vanadium solid state chemistry and has not been previously seen in BaVPOs. A similar local $\mathrm{VO}_{5}$ geometry arises in $\mathrm{KVO}_{3} \cdot \mathrm{H}_{2} \mathrm{O}(27)$ as part of a "double-chain" metavanadate $\left[\left(\mathrm{VO}_{3}\right)_{n}\right]$ ion. In this phase, there are two terminal $\mathrm{V}=\mathrm{O}$ bonds and three $\mathrm{V}-\mathrm{O}-\mathrm{V}^{\prime}$ links in the infinite double chains. One way of viewing the metavanadate double chain is in terms of the nominal fusing together of parallel chains of distorted tetrahedra (28). $\mathrm{V}_{2} \mathrm{O}_{5}$ contains a different, highly distorted $\mathrm{VO}_{5}$ grouping, which is closer to square pyramidal (29). The more common square pyramidal $\mathrm{VO}_{5}$ geometry

TABLE 5
Summary of Barium Vanadium Phosphate Phases ${ }^{a}$

| Phase | Ratio | Ox. | Coord. | Dim. | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Ba}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)$ | 1:1:1 | V | D | 2D | 4 |
| $\mathrm{Ba}(\mathrm{VO})\left(\mathrm{PO}_{4}\right)\left(\mathrm{H}_{2} \mathrm{PO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ | 1:1:2 | IV | D | 2D | 9 |
| $\mathrm{Ba}(\mathrm{VO})_{2}\left(\mathrm{PO}_{4}\right)_{2}$ | 1:2:2 | IV | D + S | 2D | 1 |
| $\mathrm{Ba}(\mathrm{VOPO} 4)_{2} \cdot 4 \mathrm{H}_{2} \mathrm{O}$ | 1:2:2 | IV | S | 2D | 11 |
| $\alpha-\mathrm{BaV}_{2}\left(\mathrm{P}_{2} \mathrm{O}_{7}\right)_{2}$ | 1:2:4 | III | O | 3D | 2 |
| $\beta-\mathrm{BaV}_{2}\left(\mathrm{P}_{2} \mathrm{O}_{7}\right)_{2}$ | 1:2:4 | III | O | 3D | 6 |
| $\mathrm{BaV}_{2}\left(\mathrm{HPO}_{4}\right)_{4} \cdot \mathrm{H}_{2} \mathrm{O}$ | 1:2:4 | III | O | 3D | 5 |
| $\mathrm{Ba}_{2}(\mathrm{VO})\left(\mathrm{PO}_{4}\right)_{2} \cdot \mathrm{H}_{2} \mathrm{O}$ | 2:1:2 | IV | D | 1D | 7 |
| $\mathrm{Ba}_{2}\left(\mathrm{VO}_{2}\right)\left(\mathrm{PO}_{4}\right)\left(\mathrm{HPO}_{4}\right) \cdot \mathrm{H}_{2} \mathrm{O}$ | 2:1:2 | V | B | 1D | This work |
| $\mathrm{Ba}_{2}(\mathrm{VO})\left(\mathrm{PO}_{4}\right)_{2}$ | 2:1:2 | IV | D | 2D | 10 |
| $\mathrm{Ba}_{2} \mathrm{~V}_{3} \mathrm{H}\left(\mathrm{PO}_{4}\right)_{2}\left(\mathrm{P}_{2} \mathrm{O}_{7}\right)_{2}$ | 2:3:6 | III | O | 3D | 3 |
| $\mathrm{Ba}_{2} \mathrm{~V}_{5} \mathrm{O}_{8}\left(\mathrm{PO}_{4}\right)_{4}$ | 2:5:4 | IV + V | T+S+D | 3D | 13 |
| $\mathrm{Ba}_{3} \mathrm{~V}_{2} \mathrm{O}_{3}\left(\mathrm{PO}_{4}\right)_{3}$ | 3:2:3 | IV + V | $\mathrm{S}+\mathrm{D}$ | 1D | 14 |
| $\mathrm{Ba}_{3} \mathrm{~V}_{4}\left(\mathrm{PO}_{4}\right)_{6}$ | 3:4:6 | III | O | 3D | $12^{\text {b }}$ |
| $\mathrm{Ba}_{8}(\mathrm{VO})_{6}\left(\mathrm{PO}_{4}\right)_{2}\left(\mathrm{HPO}_{4}\right)_{11} \cdot 3 \mathrm{H}_{2} \mathrm{O}$ | 8:6:13 | IV | D | 1D | 8 |

[^3](short, apical $\mathrm{V}=\mathrm{O}$ bond and four longer equatorial $\mathrm{V}-\mathrm{O}$ links) occurs in many inorganic phases such as $\mathrm{K}\left(\mathrm{VO}_{2}\right)$ $\left(\mathrm{HPO}_{4}\right)(30)$, which consists of one-dimensional chains of $\mathrm{VO}_{5}$ and $\mathrm{PO}_{4}$ groups, linked via $\mathrm{V}-\mathrm{O}-\mathrm{V}$ and $\mathrm{V}-\mathrm{O}-\mathrm{P}$ bonds.

Referring to Table 5, we see that vanadium(III)-containing BaVPOs are inevitably three-dimensional in their polyhedral connectivity throughout the structure, whereas the vanadium(IV) and vanadium(V) BaVPOs tend toward lower dimensionality (layers and chains). Even for a particular $\mathrm{Ba}: \mathrm{V}: \mathrm{P}$ compositional ratio, there is striking structural diversity, which is due in part to versatility of the phosphate group (its ability to form $\mathrm{P}-\mathrm{O}-\mathrm{V}, \mathrm{P}-\mathrm{O}$, or $\mathrm{P}-\mathrm{OH}$ links), and the lack of a strong coordination preference for the $\mathrm{Ba}^{2+}$ cation. However, the packing requirements of the bulky $\mathrm{Ba}^{2+}$ species in barium-rich phases (14) may also promote the formation of lower-dimensional VPO structures.

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[^1]:    ${ }^{a} I>3 \sigma(I)$ after data merging to 2029 unique reflections.
    ${ }^{b} R=100 \times \sum| | F_{\mathrm{o}}\left|-\left|F_{\mathrm{c}}\right|\right| / \sum\left|F_{\mathrm{o}}\right|$.
    ${ }^{c} R_{\mathrm{w}}=100 \times\left[\sum w\left(\left|F_{\mathrm{o}}\right|-\left|F_{\mathrm{c}}\right|\right)^{2} / \sum w\left|F_{\mathrm{o}}\right|^{2}\right]^{1 / 2}$ with $w_{\mathrm{i}}=1 / \sigma^{2}(F)$.

[^2]:    ${ }^{a} U_{\text {eq }}\left(\AA^{2}\right)=\frac{1}{3}\left[U_{1}+U_{2}+U_{3}\right]$.

[^3]:    ${ }^{a}$ Ratio, Ba:V:P ratio; Ox, V oxidation state; Coord, vanadium coordination polyhedron type $(\mathrm{O}=$ octahedral, $\mathrm{D}=$ distorted octahedral, $\mathrm{S}=$ square pyramidal, $\mathrm{B}=$ trigonal bipyramidal, $\mathrm{T}=$ tetrahedral); Dim, dimensionality of $\mathrm{V} / \mathrm{P} / \mathrm{O}$ network (3D $=$ continuous network, $2 \mathrm{D}=$ layers, $1 \mathrm{D}=$ chains).
    ${ }^{b}$ Langbeinite structure type identified from powder diffraction data.

